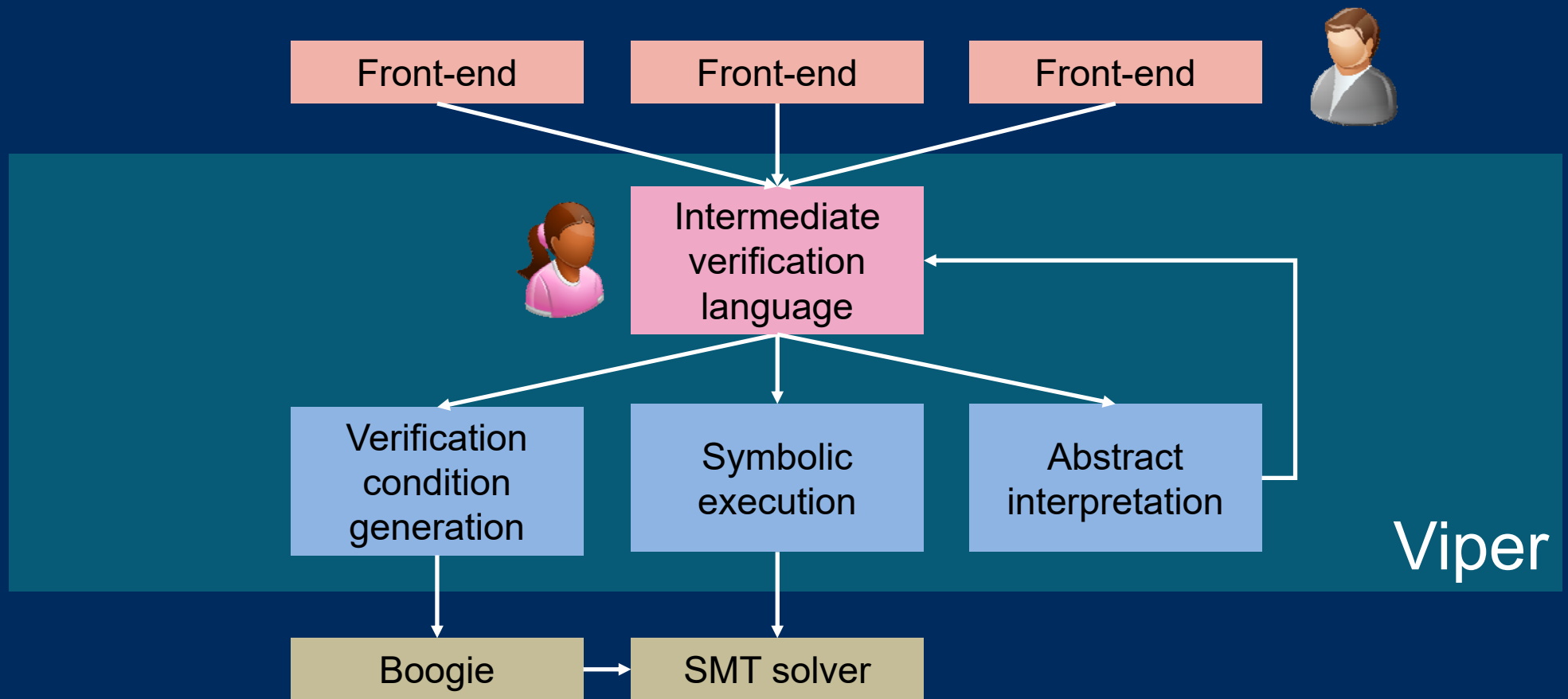


Prototyping Relaxed Separation Logic in Viper

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Separation Logic

- Heap properties are specified via points-to assertions

$$x.f \rightarrow v$$

- Each heap access to $x.f$ requires permission to $x.f$

$$\{ x.f \rightarrow _ \} x.f := v \{ x.f \rightarrow v \}$$

Separating Conjunction

- Composition of heaps is described using separating conjunction

$P * R$

- Frame rule

$$\frac{\{P\} S \{Q\}}{\{P * R\} S \{Q * R\}}$$

- Parallel composition

$$\frac{\{P_1\} S_1 \{Q_1\} \quad \{P_2\} S_2 \{Q_2\}}{\{P_1 * P_2\} S_1 \parallel S_2 \{Q_1 * Q_2\}}$$

Permission Transfer

$$\frac{\frac{\{P\} \text{ method } m \{Q\}}{\{P\} \text{ e.m() } \{Q\}}}{\{P * R\} \text{ e.m() } \{Q * R\}}$$
$$\frac{\frac{\{P_1\} S_1 \{Q_1\} \quad \{P_2\} S_2 \{Q_2\}}{\{P_1 * P_2\} S_1 \parallel S_2 \{Q_1 * Q_2\}}}{\{P_1 * P_2 * R\} S_1 \parallel S_2 \{Q_1 * Q_2 * R\}}$$

Exhale and Inhale

exhale P

- Assert all logical constraints in P
- Check and remove permissions described by P

inhale Q

- Obtain permissions described by Q
- Assume all logical constraints in Q

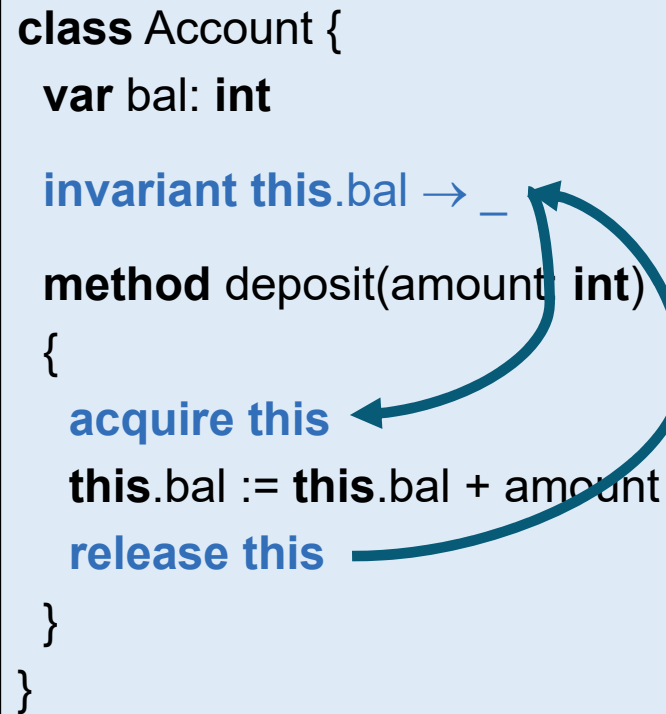
- Analogs of **assert** and **assume**

The diagram shows a sequence of three lines representing logical constraints and a method call, separated by horizontal lines. The top line is $\{P\} \text{ method } m \{Q\}$. The middle line is $\{P\} e.m() \{Q\}$. The bottom line is $\{P * R\} e.m() \{Q * R\}$. A blue arrow curves from the $\{P\}$ in the top line down to the $\{P * R\}$ in the bottom line, indicating an 'exhale' operation. A green arrow curves from the $\{Q * R\}$ in the bottom line up to the $\{Q\}$ in the middle line, indicating an 'inhale' operation.

exhale P
inhale Q

Encoding Monitors

```
class Account {  
  var bal: int  
  
  invariant this.bal → _  
  
  method deposit(amount: int)  
  {  
    acquire this  
    this.bal := this.bal + amount  
    release this  
  }  
}
```



```
inhale this.bal → _  
this.bal := this.bal + amount  
exhale this.bal → _
```

Weak Memory

- Modern hardware often does not provide sequentially consistent shared memory
- Weak memory permits behaviors that are not possible under sequential consistency
- However, data-race free programs have only sequentially consistent behaviors

```
        a = 0;  
        b = 0;  
  
a = 1;   ||   b = 1;  
print(b); ||   print(a);
```

Possible results:

under SC: 10, 01, 11

under WM: also 00

C11

- The C11 memory model provides several kinds of variables

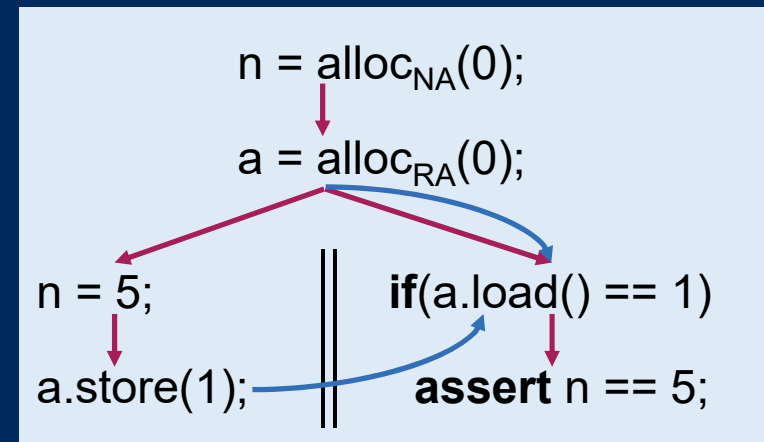
- Non-atomic variables

- Data races are errors

- Atomic variables with release-write and acquire-read

- Writes and reads are synchronized

- Relaxed separation logic (RSL) supports some features of the C11 memory model

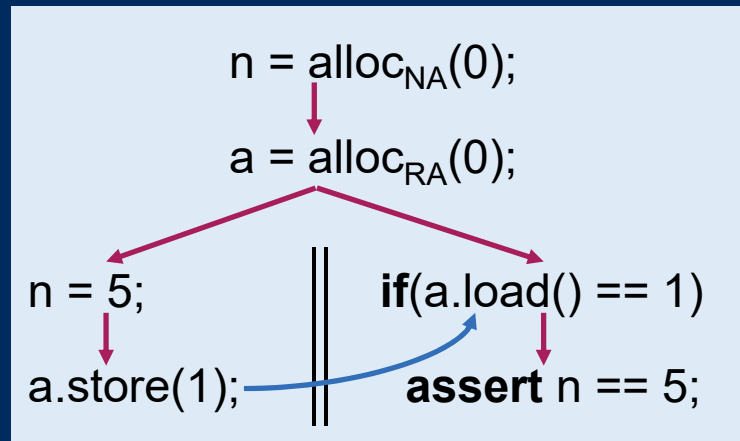


Non-Atomic Variables

- Permissions prevent data races on non-atomic variables

$$\{ \text{true} \} \ x = \text{alloc}_{\text{NA}}(v) \ \{ x \rightarrow v \}$$
$$\{ x \rightarrow _ \} \ *x = v \ \{ x \rightarrow v \}$$
$$\{ x \rightarrow V \} \ t = *x \ \{ x \rightarrow V \ * t = V \}$$

Release-Acquire

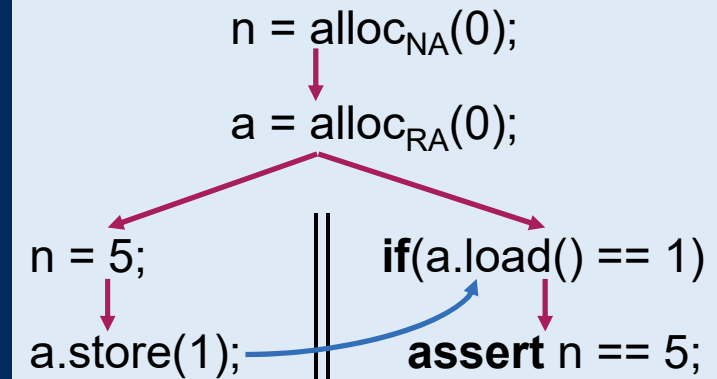


- Races on atomic variables are permitted
- Release-acquire can be seen as message passing
- Messages may transfer permissions to non-atomic variables

Location Invariants

- Location invariant $Q(v)$ specifies an assertion that holds when the location has value v
- Acquire-read of value v transfers permissions of $Q(v)$ from atomic variable to thread
- Release-write of value v transfers permissions of $Q(v)$ from thread to atomic variable

$$Q(v) \equiv \begin{cases} n \rightarrow 5 & \text{if } v = 1 \\ \text{true} & \text{otherwise} \end{cases}$$



Proof Rules

- Choose location invariant when allocating an atomic location

$$\{ Q(v) \} x = \text{alloc}_{RA}(v) \{ \text{Rel}_Q(x) * \text{Acq}_Q(x) \}$$

- Release-write gives up permissions

$$\{ \text{Rel}_Q(x) * Q(v) \} x.\text{store}(v) \{ \text{Rel}_Q(x) \}$$

- Acquire-read gains permissions

$$\{ \text{Acq}_Q(x) \} t = x.\text{load}() \{ Q(t) * \text{Acq}_Q(x) \}$$

Proof Rules

$$\{ \text{Acq}_Q(x) \} \ t = x.\text{load}() \ \{ Q(t) * \text{Acq}_{Q[t := \text{true}]}(x) \}$$

- Reading the same value more than once would duplicate permissions

$$Q(v) \equiv \begin{cases} n \rightarrow 5 & \text{if } v = 1 \\ \text{true} & \text{otherwise} \end{cases}$$

```
x = a.load();  
y = a.load();  
if(x == y)  
    assert false;
```

Proof Outline

```
    { true }  
    n = allocNA(0);  
    { n → 0 }  
    a = allocRA(0);  
    { n → 0 * RelQ(a) * AcqQ(a) }
```

```
{ n → 0 * RelQ(a) }
```

```
  n = 5;
```

```
{ n → 5 * RelQ(a) }
```

```
  a.store(1);
```

```
{ RelQ(a) }
```



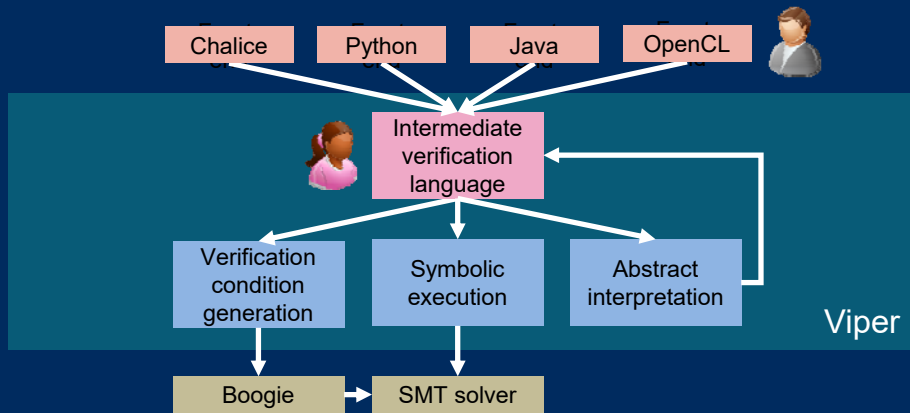
```
{ AcqQ(a) }
```

```
if(a.load() == 1)
```

```
{ Q(1) * AcqQ(a) }
```

```
  assert n == 5;
```

$$Q(v) \equiv \begin{cases} n \rightarrow 5 & \text{if } v = 1 \\ \text{true} & \text{otherwise} \end{cases}$$

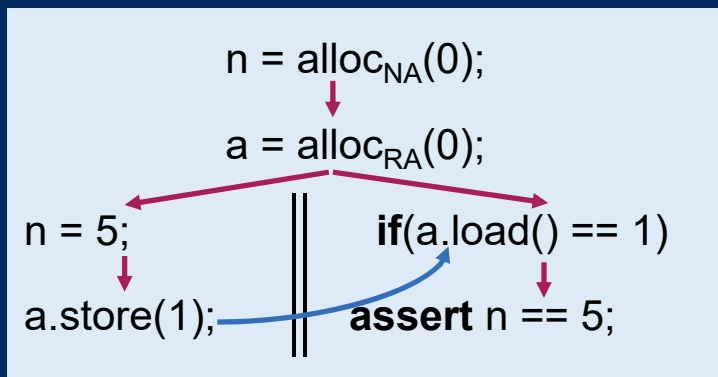


Intermediate languages enable prototyping and reuse of infrastructure

$$\frac{\{P\} S \{Q\}}{\{P * R\} S \{Q * R\}}$$

$$\frac{\{P_1\} S_1 \{Q_1\} \quad \{P_2\} S_2 \{Q_2\}}{\{P_1 * P_2\} S_1 \parallel S_2 \{Q_1 * Q_2\}}$$

Permissions enable framing and reasoning about concurrency



RSL proof rules can be encoded into Viper



viper.ethz.ch